

# Quiz 6, Linear

Name: \_\_\_\_\_

1. (4 points) If the equation  $G\mathbf{x} = \mathbf{y}$  has more than one solution for some  $\mathbf{y}$  in  $\mathbb{R}^n$ , can the columns of  $G$  span  $\mathbb{R}^n$ ? Why or why not?

2. (2 points) Let  $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ . Prove that  $\det(kA) = k^2(\det A)$  where  $k$  is any real number.

3. (4 points) Calculate  $\det A$  for  $A = \begin{bmatrix} 4 & 0 & -7 & 3 & -5 \\ 0 & 0 & 2 & 0 & 0 \\ 7 & 3 & -6 & 4 & -8 \\ 5 & 0 & 5 & 2 & -3 \\ 0 & 0 & 9 & -1 & 2 \end{bmatrix}$ .